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Title: Unknotting number 21 knots are slice in $K3$

Abstract: A question in knot theory that has become very popular recently is to classify what knots bound a smooth disc in $X - int(B^4)$, where X is a given closed 4-manifold. We study the case when X is the $K3$ surface, and prove that every knot that can be unknotted with at most 21 crossing changes, bounds a smooth disc in $K3 - int(B^4)$. Our proof is constructive and based on the existence of a plumbing tree of 22 spheres in $K3$. We present a simple but flexible technique to simultaneously remove multiple singularities of immersed surfaces in 4-manifolds.