Conflict-free coloring of graphs

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(joint work with Roman Glebov and Tibor Szabó)

Conflict-free chromatic number of hypergraphs was introduced Even *et al.* and was motivated by a frecvency assignment problem. We study this parameter of the neighborhood hypergraphs of graphs from extremal and probabilistic points of view. We resolve a question of Pach and Tardos about the maximum conflictfree chromatic number the neighborhood hypergraph of an *n*-vertex graph can have. Our construction is randomized. In relation to this we study the evolution of the conflict-free chromatic number of the Erdős-Rényi random graph G(n, p)and give the asymptotics for $p = \omega(1/n)$. We also show that for $p \ge 1/2$ the conflict-free chromatic number differs from the domination number by at most 3.