

On the Richter-Thomassen Conjecture about Pairwise Intersecting Curves

Natan Rubin*

Abstract

Let Γ be a family of n closed Jordan curves in the plane, where any two curves are either tangent or properly intersecting. We discuss a long standing conjecture of Richter and Thomassen which suggests, in its somewhat stronger form, that the overall number of intersection points among the curves of Γ must be strictly larger in asymptotic terms than the number of touching pairs of curves in Γ (as n tends to infinity).

We confirm the above conjecture in several important cases including x -monotone curves or, more generally, curves which can be decomposed into constantly many x -monotone pieces.

This is joint work in progress with János Pach and Gábor Tardos.

*Université Pierre & Marie Curie, Institut de Mathématiques de Jussieu (UMR 7586), 4 Place Jussieu, 75252 Paris Cedex, France. Email: rubinnat.ac@gmail.com.