Graphs with and without cycles

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A well known question of Erdős asks: How many pentagons can there be in a triangle free graph? We consider a couple of variants to this problem in both graphs and hypergraphs. We discuss a connection to the problem of relating the extremal sizes of graphs excluding a cycle of length $2k$ and graphs of girth at least $2k + 1$.